

Course Outline

I. Introduction

- A. Importance of fluid flow, prevalence of turbulence
- B. Descriptions of turbulence
- C. History of study of turbulence
- D. Definitions, mathematical tools, basic concepts

II. Statistical Analysis and Modeling of Turbulence

- A. Why a statistical approach?—basic notions
- B. Derivation of Reynolds-averaged Navier–Stokes (RANS) equations
- C. Discussion of lack of time dependence
- D. Vortex stretching and Reynolds stresses
- E. General difficulties with RANS—independent of specific models
- F. Description and comparison of various RANS models
 - 1. mixing length theory, van Driest model
 - 2. eddy viscosity transport
 - 3. $k-\varepsilon$ models
 - 4. second-order closures
 - 5. PDF models (if time permits)
- G. Kolmogorov's K41 theory and consequences

III. The Navier–Stokes Equations as a Dynamical System

- A. Discussion of general concepts from dynamical systems and their relation to turbulence
- B. Direct numerical simulation (DNS)
- C. Large-eddy simulation (LES)
 - 1. basic formulation
 - 2. advantages/disadvantages (compared with DNS and RANS)
 - 3. detached-eddy simulation (DES)
- D. Subgrid-scale (SGS) models
 - 1. Smagorinsky model
 - 2. dynamic models
 - 3. synthetic-velocity models

Grading

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| <u>Written</u> summaries of reading assignments | 15% |
| Homework problems (4 or 5 of varying weight) | 40% |
| Term project | 45% |

Required Texts

H. Tennekes and J. L. Lumley, *A First Course in Turbulence*, MIT Press, Cambridge, MA, 1972.

U. Frisch, *TURBULENCE, the Legacy of A. N. Kolmogorov*, Cambridge University Press, 1995.

Office Hours

Whenever you can find me, or by appointment—send e-mail to jmmcd@uky.edu.